

# Privacy-Enhancing Proxy Signatures from Non-Interactive Anonymous Credentials

David Derler, Christian Hanser, and Daniel Slamanig

[david.derler](mailto:david.derler@iaik.tugraz.at), [christian.hanser](mailto:christian.hanser@iaik.tugraz.at), [daniel.slamanig](mailto:daniel.slamanig@iaik.tugraz.at) @iaik.tugraz.at

Institute for Applied Information Processing and  
Communications, Graz University of Technology

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# Outline

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- Privacy-enhancing proxy signatures
  - Blank Digital Signatures [HSa]
  - Warrant-Hiding Proxy Signatures [HSb]
  - Applications

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  - Anonymous credentials
    - Brands' credentials [Bra00]
    - CL credentials [CLa]
  - Non-interactive anonymous credentials

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- Our BDS/WHPS constructions
- Conclusion

# Privacy-Enhancing Proxy Signatures

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Originator 

Proxy 

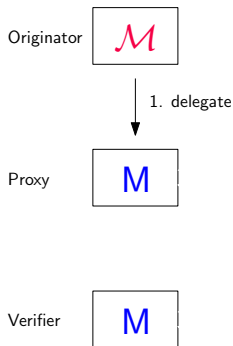
Verifier 

# Privacy-Enhancing Proxy Signatures

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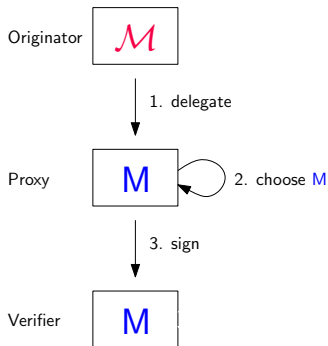
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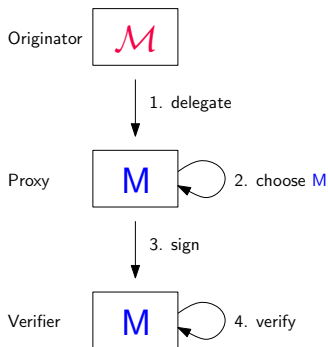
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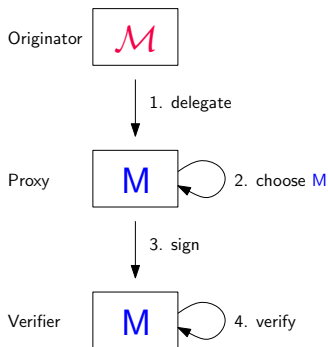


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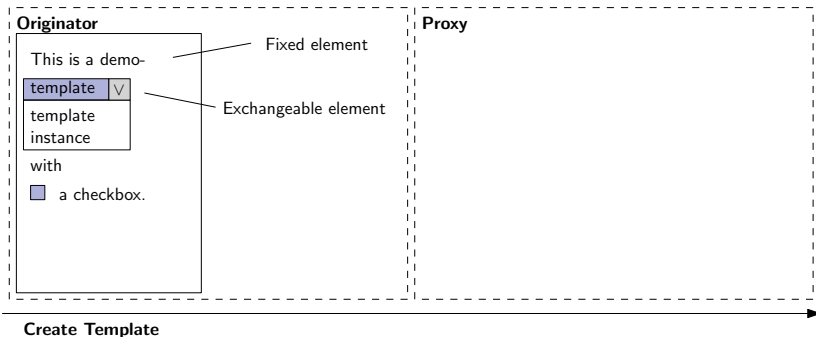
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- New: **Privacy property**
  - Hides  $\mathcal{M} \setminus M$

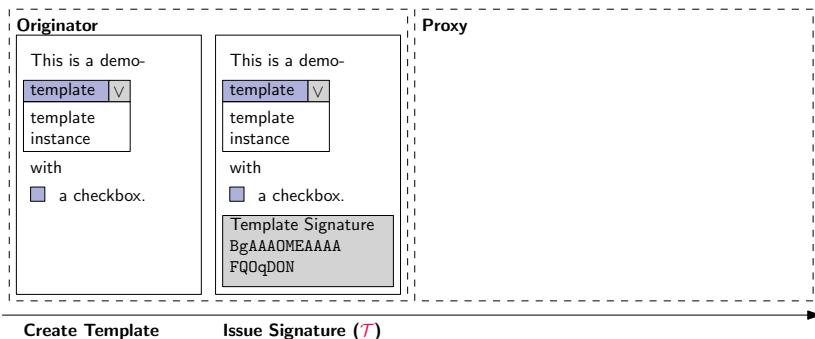
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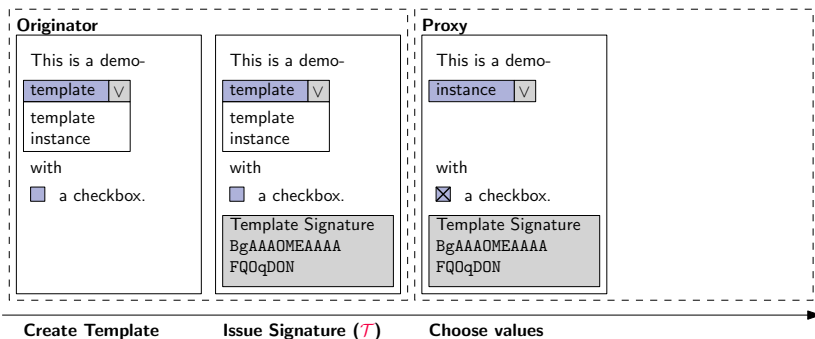
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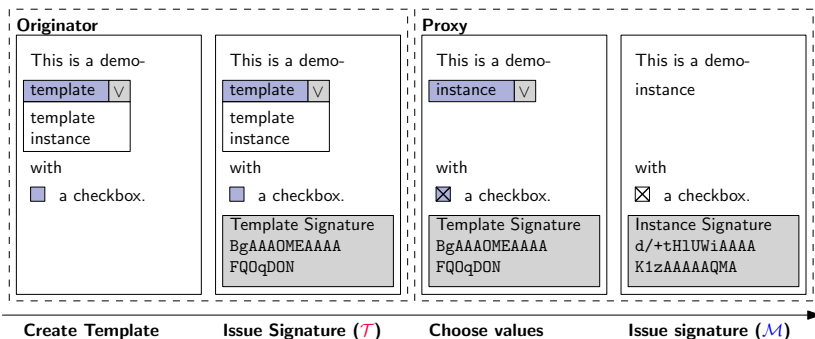
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# BDS Template/Message Representation

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- Template  $\mathcal{T} = (T_1, T_2, \dots, T_n)$  with  $T_i = \{M_{i_1}, M_{i_2}, \dots, M_{i_k}\}$

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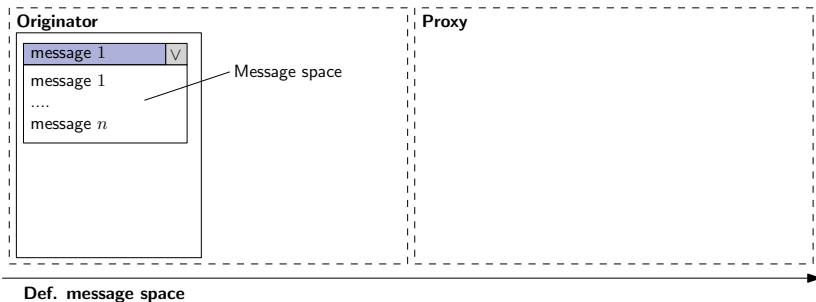
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Verifier does not learn unused choices in the template

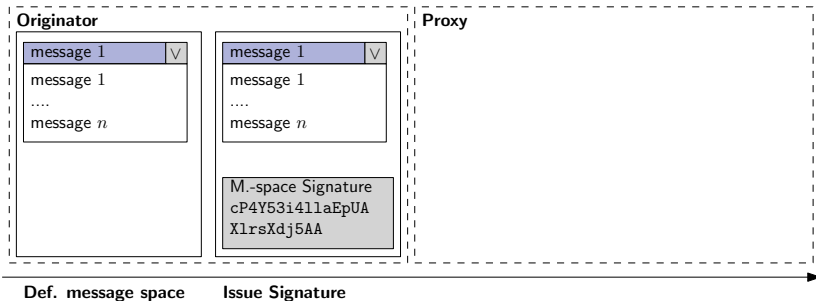
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- Message space defined by set of messages



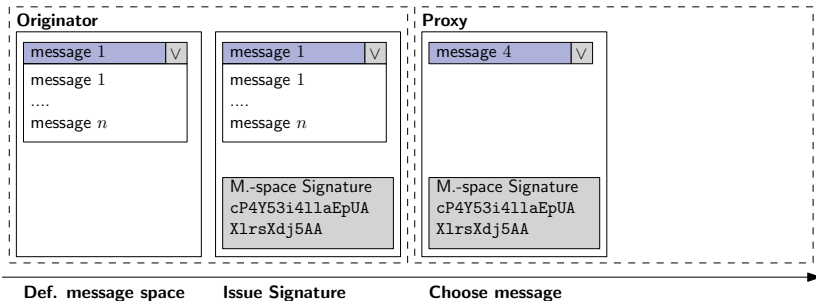
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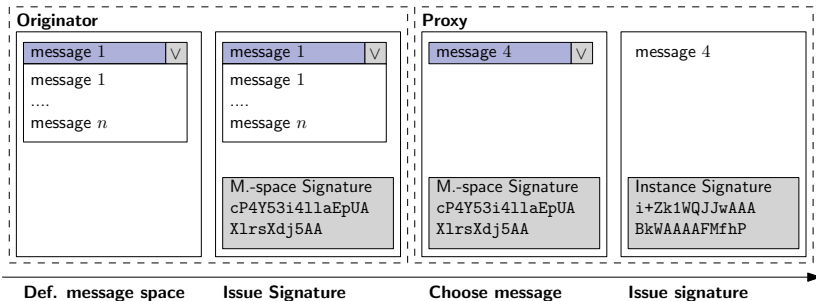
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- Message  $M = M_i, 1 \leq i \leq n$

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Verifier does not learn unrevealed messages in the warrant.

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- Attorney makes business deal
  - ... on behalf of the client
  - Privacy property

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 $\mathcal{T} =$   
({" I, hereby, declare to pay " },  
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- Warrant-Hiding Proxy Signatures
  - Subset of BDS use cases

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- Parties: Organization  $o$ , Users  $u_i$
- Organization issues credentials to users
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- Users can then anonymously demonstrate possession
  - and, thereby, selectively disclose a subset of attributes

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## Selective Disclosure

- Verifier learns nothing about non-shown attributes
- Informal requirement of all AC systems
- All known AC systems employ proofs of knowledge
  - Nothing beyond the shown attributes revealed by definition

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- Showing
  - Verify blind signature
  - Prove knowledge of DLREP
  - Multiple showings are linkable

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- Showing
  - Verify re-randomized signature
  - Prove knowledge of attributes in  $C$
  - Multiple showings unlinkable
    - Not needed in our context

# Obtaining Non-interactive AC

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- Honest-verifier zero-knowledge proofs used upon show
  - e.g., demonstrate knowledge of  $x = \log_P Y$  to base  $P$
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- Non-interactive AC Versions
  - Apply Fiat-Shamir transform [FS] to proofs
- Non-interactive Proof
  - ... together with proving knowledge of a secret key
  - Secure digital signature in the random oracle model [CLb]
  - Interpreted as the proxy's signature

# Bringing it Together

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- Why not use this for BDS/WHPS?
  - Encode template elements/message space within attributes
  - Provide non-interactive showings
    - Reveal subset of the attributes
    - Prove knowledge of secret key and remaining attributes

# BDS Encoding

---

- Template uniquely defined by its elements
  - Fixed elements
    - Position  $i$  in the template
    - Corresponding message  $m_i$
  - Exchangeable elements
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- Template element  $\mapsto$  AC attribute

$$\mathcal{T} = (\{m_{1_1}\}, \{m_{2_1}, m_{2_2}, m_{2_3}\})$$
$$\mathcal{T}^{\text{enc}} = (H(m_{1_1}||1), \underset{\downarrow}{H(m_{2_1}||2)}, H(m_{2_2}||2), H(m_{2_3}||2))$$



## BDS Encoding (2)

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- Template instantiation

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- Encode number of elements  $l$  into first attribute
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- Ensure that one attribute  $m_{i_j}$  is shown for each  $1 \leq i \leq l$

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# WHPS Encoding

---

- Message space  $\mathcal{M}$  defined by contained messages  $m_i$
- Encoding a lot simpler
  - No order of messages in the message space
  - Random permutation not needed
  - ... no useful information leaks
- $\mathcal{M} = \{m_1, \dots, m_n\} \mapsto (H(m_1), \dots, H(m_n))$
- Instantiation:  $\{\blacksquare, \dots, \blacksquare, \dots, H(m_i), \dots, \blacksquare\}$

# Modeling the Delegation

---

- Keys compatible with system parameters of used ACs
  - Secret key  $sk \in \mathbb{Z}_p^*$
  - Public key  $pk = sk \cdot P$  ( $P$  generates used group  $\mathbb{G}$ )

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- Possible for Brands' and CL credentials
- If not
  - Incorporate public key as attribute
  - Prove knowledge by providing a signature

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  - Basis for practical implementations
- Flexibility regarding underlying constructions
- First approach to build special signature schemes from AC
  - Inspiration for other constructions
- Proposed encoding might also be useful for AC



# Thank you.

david.derler@iaik.tugraz.at

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